## Projeto 4: Transformações do Plano

## Objetivo

Dar alguma experiência com geometria de algumas transformações simples no plano.

## Resumo

Neste projeto é mostrada a geometria de algumas transformações simples no plano aplicado a um padrão teste simples.

## Tarefa:

a) Reproduza o trecho de planilha Mathcad abaixo. Ele define o padrão teste.

$$i := 0..100$$

$$L1x_i := \frac{i}{100}$$
  $L1y_i := 0$   $L2x_i := 0$   $L2y_i := \frac{i}{100}$   $L3x_i := 1$   $L3y_i := \frac{i}{100}$ 

$$L2x_i := 0$$

$$L2y_i := \frac{i}{100}$$

$$L3x_i := 1$$

$$L3y_i := \frac{i}{100}$$

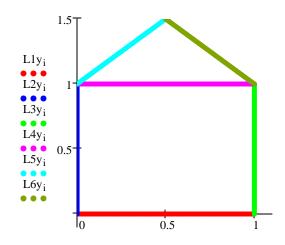
$$L4x_{i} := \frac{i}{100}$$

$$L4y_i := 1$$

$$L5x_{\underline{i}} := \frac{i}{200}$$

$$L5y_i := 1 + \frac{1}{20}$$

$$L4x_{\underline{i}} := \frac{i}{100} \qquad L4y_{\underline{i}} := 1 \qquad L5x_{\underline{i}} := \frac{i}{200} \qquad L5y_{\underline{i}} := 1 + \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6y_{\underline{i}} := 1.5 - \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6y_{\underline{i}} := 1.5 - \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6y_{\underline{i}} := 1.5 - \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6y_{\underline{i}} := 1.5 - \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6y_{\underline{i}} := 1.5 - \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6y_{\underline{i}} := 1.5 - \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6y_{\underline{i}} := 1.5 - \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6y_{\underline{i}} := 1.5 - \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6y_{\underline{i}} := 1.5 - \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6y_{\underline{i}} := 1.5 - \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6y_{\underline{i}} := 1.5 - \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6y_{\underline{i}} := 1.5 - \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6y_{\underline{i}} := 1.5 - \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6y_{\underline{i}} := 1.5 - \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6y_{\underline{i}} := 1.5 - \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6y_{\underline{i}} := 1.5 - \frac{i}{200} \qquad L6x_{\underline{i}} := \frac{i}{200} + 0.5 \qquad L6x_{\underline{i}} := \frac{i}{200}$$



L1x<sub>i</sub>, L2x<sub>i</sub>, L3x<sub>i</sub>, L4x<sub>i</sub>, L5x<sub>i</sub>, L6x<sub>i</sub>

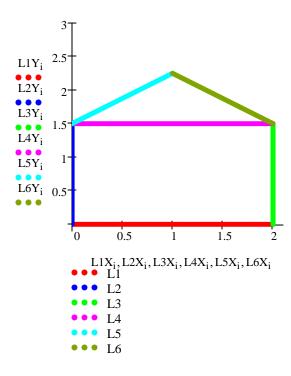
L1

2) Reproduza o trecho de planilha abaixo. Ele define a transformação  $T(x,y) \rightarrow (2x, 1.5y)$  e mostra a imagem transformada do padrão teste.

$$\mathsf{L1X}_{\mathbf{i}} \coloneqq 2 \cdot \mathsf{L1x}_{\mathbf{i}} \qquad \mathsf{L1Y}_{\mathbf{i}} \coloneqq 1.5 \cdot \mathsf{L1y}_{\mathbf{i}} \qquad \qquad \mathsf{L2X}_{\mathbf{i}} \coloneqq 2 \cdot \mathsf{L2x}_{\mathbf{i}} \qquad \mathsf{L2Y}_{\mathbf{i}} \coloneqq 1.5 \cdot \mathsf{L2y}_{\mathbf{i}}$$

$$L3X_{i} := 2 \cdot L3x_{i}$$
  $L3Y_{i} := 1.5 \cdot L3y_{i}$   $L4X_{i} := 2 \cdot L4x_{i}$   $L4Y_{i} := 1.5 \cdot L4y_{i}$ 

$$L5X_{i} := 2 \cdot L5x_{i}$$
  $L5Y_{i} := 1.5 \cdot L5y_{i}$   $L6X_{i} := 2 \cdot L6x_{i}$   $L6Y_{i} := 1.5 \cdot L6y_{i}$ 



3) Repita a tarefa 2 usando aa transformações:

a) 
$$T(x,y) \rightarrow (-x, y)$$

d) 
$$T(x,y) \rightarrow (x-y+3, 2x+y)$$

b) 
$$T(x,y) \to (x+2, y+1)$$

e) 
$$T(x,y) \to (x+2, x^2 + y)$$

c) 
$$T(x,y) \rightarrow (\frac{\sqrt{2}}{2}(x-y), \frac{\sqrt{2}}{2}(x+y))$$

4) Adicione uma porta e uma janela ao padrão teste e repita tudo o que foi feito.

Seu relatório será a planilha que você digitou e as respostas Mathcad, e também as respostas para parte (4).